

2023

CONTROL SYSTEM

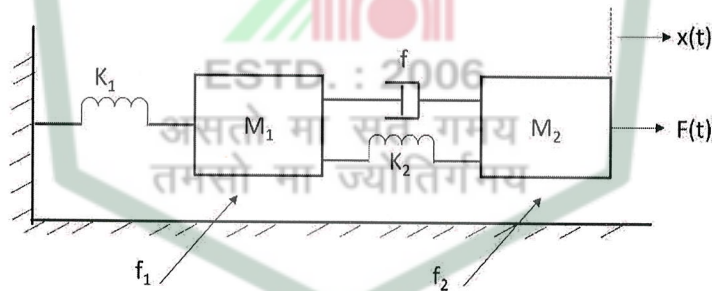
Full Marks : 100

Time : Three hours

The figures in the margin indicate full marks for the questions.

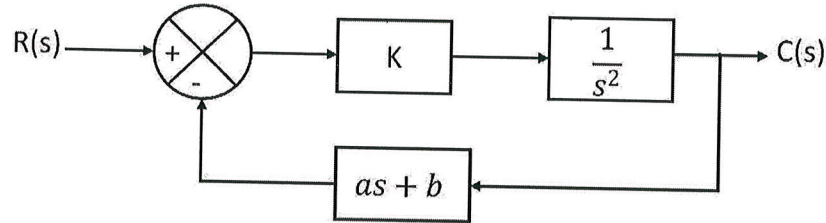
Answer any five questions.

1. a) Write the definitions of the following with suitable examples. 2×3
- i) System
 - ii) Controlled system
 - iii) Transfer Function
- b) What is analogous system? Obtain analogous relationships among mechanical and electrical system. 6
- c) Obtain the analogous electrical circuits based on 4+4
- a) Force-current analogy
 - b) Force-voltage analogy.

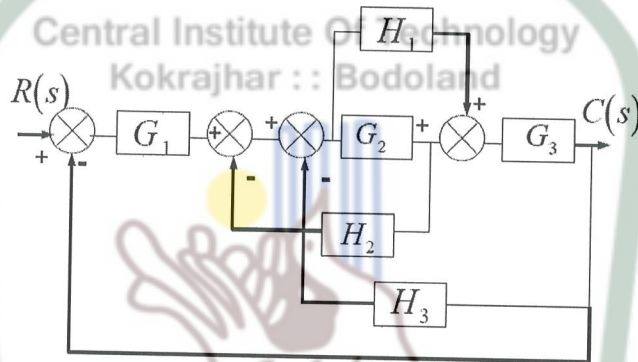


2. a) Define the three steady state error for a control system. 2
- b) For a unity feedback system having open loop transfer function as 1+3+4
- $$G(s) = K(s+2)/s^2 (s^2 + 7s+ 12),$$
- determine i) Type of the system, ii) Error constants, iii) Steady state error for parabolic input.
- c) Obtain the time response expression of a first order control system 5+5
- subjected to unit step and unit ramp input.

3. a) The block diagram of a simple servomechanism is shown in the following figure. Determine the value of 'a' and 'b' to provide an overshoot of 16% with time constant of 0.1 sec for a unit step input. Find also the damping ratio when $K = 40$. 6



- b) Write the rules for simplification of the block diagram algebra. 6
- c) Simplify the block diagram and find the overall transfer function. 8



4. a) State the Routh stability criterion. Using the Routh's stability criterion, calculate the range of 'K' for which the following system become stable for unity feedback. 2+4

$$G(s) = \frac{K(s+13)}{s(s+3)(s+7)}$$

- b) What is Mason's gain formula? Represent the following set of equations by a signal flow graph and determine the overall transfer function using Mason's gain formula. 4+5

$$x = x_1 + \alpha_3 u$$

$$\dot{x}_1 = -\beta_1 x_1 + x_2 + \alpha_2 u$$

$$\dot{x}_2 = -\beta_2 x_1 + \alpha_1 u$$

- c) Explain the concept of stability of a control system. 5

5. a) Why root locus plot is necessary in control system? Discuss two basic conditions for plotting a root locus. 5

- b) A unity feedback control system has an open-loop transfer function 15

$$G(s)H(s) = \frac{K(s+1)}{s^2 + 0.4s + 0.4} . \text{ Sketch the root locus plot of the system.}$$

Determine the value of K at $s = -2$. Comment on the stability and time response of the system.

6. Write short notes on any four from the following topics. 5x4=20

- a) Transient Response Specifications
- b) Lag compensator
- c) State model of linear system
- d) Observability of a system
- e) State transition matrix

7. a) Consider an open loop unstable system with the transfer function 10

$$G(s)H(s) = \frac{(s+2)}{(s+1)(s-1)} . \text{ Determine system stability when the feedback path is closed using Nyquist stability criterion.}$$

- b) Sketch the asymptotic Bode plot for the following transfer function 10

$$G(s)H(s) = \frac{2(s+0.25)}{s^2(s+1)(s+0.5)} .$$

From the Bode plot determine

- i) Phase cross over frequency
- ii) Gain cross over frequency
- iii) Gain margin
- iv) Phase margin