

2023
FUNDAMENTALS OF HEAT AND MASS TRANSFER

Full Marks : 100

Time : Three hours

The figures in the margin indicate full marks for the questions.

Answer any five questions.

1. a) Write Fick's first law of diffusion. 4
- b) How diffusivity varies with temperature, pressure, molecular weight, molecular size? 6
- Mention diffusivity range of solute in gas and liquid phase at ambient temperature.
- c) A molecule is being transported by diffusion through a fluid at steady state. At a given point 1, concentration is $1.37 \times 10^{-2} \text{ g/m}^3$ and $0.72 \times 10^{-2} \text{ g/m}^3$ at point 2. The distance in between is 0.4 m. Diffusivity $0.013 \text{ m}^2/\text{s}$ and cross sectional area is constant. Calculate flux. Derive the equation for concentration as a function of distance. Calculate concentration at the middle point of 1 and 2. 10
2. a) What is interphase mass transfer? 5
- b) The equilibrium distribution of a solute (O_2) between air and water at low concentration at a particular temperature is given by $y=1.2x$ 15
- At a certain point in a mass transfer device, the concentration of solute in bulk air is 0.04 mole fraction and in bulk liquid phase is 0.025. The individual mass transfer coefficients are $k_y= 7.2 \text{ kmol/h m}^2$ and $k_s= 4.6 \text{ kmol/h m}^2$.
- Calculate
- In which direction solute transport will happen?
- Overall gas phase and overall liquid phase driving force for mass transfer.
- Interfacial concentration in gas & liquid phase.
- Flux N_A
- Overall mass transfer coefficients K_x & K_y .
- Which resistance controls the mass transfer?

- 3 a) Write solute transfer process for the following unit operation: 5
- Absorption
- Adsorption
- Liquid –liquid extraction
- Leaching
- Distillation
- b) What is countercurrent multiple equilibrium contact stages for solute transfer. 10
Discuss briefly with graphical plot for theoretical stages required for separation.
- c) A polyethylene film 0.15 mm thick is considered for packaging for pharmaceutical product at 30 °C. The partial pressure of oxygen outside is 0.21 atm and inside is 0.01 atm. Calculate the permeation flux of oxygen through the film at steady state. Permeability $PM = 4.17 \times 10^{-12} \text{ m}^3/\text{s m}^2 \text{ atm/m}$. 5
4. a) Explain Thermal Resistance 3
- b) Calculate the rate of heat transfer per unit area through a copper plate 45 mm thick, whose one face is maintained at 350 °C and the other face at 50 °C. Take thermal conductivity of copper as 370 W/m °C. 4
- c) Derive **Fourier's Equation** 10
- $$\nabla^2 t = \frac{1}{\alpha} \cdot \frac{\partial t}{\partial \tau}$$
- ESTD. : 2006
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- For Unsteady heat conduction through a homogeneous and isotropic material without internal heat generation.
- d) Consider a slab of thickness $L = 0.25 \text{ m}$. One surface is kept at 100 °C and the other surface at 0 °C. Determine the heat transfer per unit area across the slab if the slab is made from pure copper. Thermal conductivity of copper may be taken as 387.6 W/m K. 3
5. a) A furnace wall is composed of **220 mm** of fire brick, **150 mm** of common brick, **50 mm** of 85% magnesia and 3 mm of steel plate on the outside. If the inside surface temperature is **1500 °C** and outside surface temperature is **90 °C**, estimate the temperatures between layers and calculate the heat loss in kJ/h-m^2 . Assume k (for fire brick) = 4 $\text{kJ/m-h-}^\circ\text{C}$, k (for common brick) = **2.8** $\text{kJ/m-h-}^\circ\text{C}$, k (for 85% magnesia) = **0.24** $\text{kJ/m-h-}^\circ\text{C}$, and k (for steel) = **240** $\text{kJ/m-h-}^\circ\text{C}$ 5

- b) Show that heat conduction through a composite layer of 'n' numbers of concentric cylinders is 6

$$Q = \frac{2\pi L(t_{hf} - t_{cf})}{\left[\frac{1}{h_{hf} \cdot r_1} + \frac{\ln(r_2/r_1)}{k_A} + \frac{\ln(r_3/r_2)}{k_B} + \frac{1}{h_{cf} \cdot r_3} \right]}$$

- c) A steam pipe of outer diameter 120 mm is covered with two layers of lagging, inside layer 45 mm thick ($k = 0.08 \text{ W/m } ^\circ\text{C}$) and outside layer 30 mm thick ($k = 0.12 \text{ W/m } ^\circ\text{C}$). The pipe conveys steam at a pressure of 20 bar and temperature $262.4 \text{ } ^\circ\text{C}$. The outside temperature of lagging is $25 \text{ } ^\circ\text{C}$. If the steam pipe is 30 m long, determine: 6
- (i) Heat lost per hour.
- (ii) Interface temperature of lagging.
- d) Explain logarithmic mean area for hollow sphere. 3
6. a) Explain critical thickness of insulation for a hollow cylinder and its physical significance. 5
- b) A uniform sheathing of plastic insulation ($k = 0.18 \text{ W/m } ^\circ\text{C}$) is applied to an electric cable of 8 mm diameter. The convective film coefficient on the surface of bare cable as well as insulated cable was estimated at $12.5 \text{ W/m}^2 \text{ } ^\circ\text{C}$ and a surface temperature of $45 \text{ } ^\circ\text{C}$ was observed when the cable was exposed to ambient air $20 \text{ } ^\circ\text{C}$. Determine: 5
- (i) The thickness of insulation to keep the wire as cool as possible
- (ii) The surface temperature of insulated cable if the intensity of current flowing through the conductor remains unchanged.
- c) What is Logarithmic Mean Temperature Difference (LMTD) for a Heat Exchanger? 10
What are the necessary assumptions required to be made in deriving an expression for LMTD. Derive the expression for LMTD for a parallel flow heat exchanger
7. Write short notes on **any five** of the following. 20
- a) Various modes of Heat Transfer
- b) Heat Conduction through a composite wall
- c) Heat Conduction through a hollow sphere
- d) Critical thickness for a hollow sphere

- e) Types of heat exchangers based on relative direction of fluid motion
- f) Effectiveness of a heat exchanger
- g) Number of Transfer Units (NTU)

