

Total number of printed pages: Programme(UG)/5<sup>th</sup> Semester/UCSE503

2022

**FORMAL LANGUAGE AND AUTOMATA THEORY**

Full Marks : 100

Time : Three hours

The figures in the margin indicate full marks for the questions.

Answer any five questions.

Q1.

a) Construct DFA for the following where the  $\Sigma = \{x, y\}$ :

i) All strings end with  $x$  followed by  $y$ .

ii) All strings where there are three  $y$ .

iii) All strings where the number of  $x$  and  $y$  are even respectively.

iv) All strings where the number of  $x$  is odd but the number of  $y$  is even.

b) Show that a language  $L$  where  $L = x^n$  and  $n > 3$  is regular.

((3+3+4) + 6)

Q2.

a) Consider the following state transition table of a DFA and minimize it (if possible). In the following DFA  $q_0$  is the initial state and both  $q_3$  and  $q_5$  are final state.

	Input = a	Input = b
$q_0$	$q_1$	$q_3$
$q_1$	$q_0$	$q_3$
$q_2$	$q_1$	$q_4$
$q_3$	$q_5$	$q_5$
$q_4$	$q_5$	$q_5$
$q_5$	$q_3$	$q_3$

b) Design a right and left linear grammar for the language  $L$ , where  $L = a^m b^n$  and  $m > 2$  and  $n > 3$ .

(10+10)

Q3. Consider the following languages and prove whether they are regular or not

i)  $L = a^m b^n c^p$ , where  $p = m + n$ .

ii)  $L = a^m b^n c^p$  where  $m > n > p$ .

iii)  $L = a^m$  where  $m$  is always a prime number.

iv)  $L = a^m$  where  $m$  is always an even number.

(5+5+5+5)

Q4.

a) Consider the following grammar and convert it into i) Chomsky Normal form and ii) Greibach Normal Form –

$S \rightarrow aababA|a$

$A \rightarrow ABC|a$

$B \rightarrow BC|b$

$C \rightarrow y$

b) Consider the language  $L = a^n b^{3n} c^{2n}$ ,  $n > 0$ . Do you think the language  $L$  is context-free? Justify.

((6+6) +8)

Q5. Design a context-free grammar for the language  $L = a^{3n} b^{2n}$ ,  $n > 0$ . Construct a PDA that can accept  $L$ . Trace your PDA for the input string  $w$ , where  $w = aaaaaaaaaabbbbbbb$ .

(3+12+5)

Q6. Construct a TM that can accept the language  $L = a^{4n} b^n c^{3n}$ ,  $n > 0$ . Clearly write your logic and trace with any string that belongs to  $L$ .

(10+5+5)

Q7. Write short notes on the followings –

a) Recursive vs. Recursive Enumerable

b) Halting problem of TM

c) DFA vs NFA

d) Mealy vs Moore Machine

(5\*4)