

Sc-202/Maths-II/2nd Sem/Comm/2017/M

MATHEMATICS - II

Full Marks - 70

Pass Marks - 21

Time - Three hours

The figures in the margin indicate full marks for the questions.

GROUP - A

1. (a) If $f(x) = 1 + e^x$, find f(f(x)).

(b) Find the domain of the function $f(x) = \sqrt{x^2 - 1}$.

(c) Examine the continuity of f(x) where

$$f(x) = \frac{|x-1|}{x-1} \text{ if } x \neq 1$$
$$= 0 \text{ if } x = 1$$
$$at x = 1.$$

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2

2

3



2. Find the limit (any two) :

(a) Lt
$$\frac{\sqrt{x-3}}{x-9}$$

(b)
$$\lim_{x\to 0} \frac{\tan \frac{x}{3}}{x}$$

(c) Lt
$$\frac{4x^2 - 5x + 1}{5x^2 + 2x + 3}$$

3. Find
$$\frac{dy}{dx}$$
 (any three):
(a) $y = e^{f(x)}$
(b) $y = \frac{e^x}{2+x}$
(c) $x^y = y^x$
(d) $x = a$ (t + sin t), $y = b \cos t$
4. Find $\frac{d^2y}{dx^2}$ (any two):
(a) $y = e^x \tan x$
(b) $y = \cos^{-1} x$
(c) $y = \sin^5 x \cos x$

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(2)

- 5. Find the equation of the tangent to the curve $\sqrt{x} + \sqrt{y} = 3$ at (4, 1).
- 6. Find the extreme values of the function $f(x) = 2x^3 - 9x^2 + 12x + 5.$

GROUP – **B**

- 7. Integrate any three :
 - (a) $\int (\cos x)^2 dx$

(b)
$$\int \left(x^2 + \frac{1}{x^2}\right)^3 dx$$

(c)
$$\int x^2 \log x \, dx$$

(d)
$$\int \frac{\cos x}{1+\sin^2 x} dx$$

8. Evaluate any two :

(a)
$$\int_0^1 x e^x dx$$

(b)
$$\int_0^1 \frac{\tan^{-1} x}{1+x^2} dx$$

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3×2=6

(3)

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3×2=6

3

(c)
$$\int_0^{\frac{\pi}{2}} \frac{\sin x}{\sin x + \cos x} dx$$

9. Find by the method of integration the area of the region bounded by the parabola $y^2 = 8x$ and its latus rectum. 3

3

10. Find the sum :

2

Lt
$$n \left[\frac{1}{n^2 + 1^2} + \frac{1}{n^2 + 2^2} + \dots + \frac{1}{n^2 + n^2} \right]$$

GROUP – C

11. Answer any seven questions : 7×2=14

- (a) Find the centroid of the triangle with vertices(0, 0), (2, 4), (4, 0).
- (b) Show that the points (4, 4), (6, 2) and (7, 1) are collinear.
- (c) Find the equation of the straight line parallel to x = 2y and passing through (1, 1).
- (d) Find intercepts on axes by the straight line 2x + 3y 5 = 0.

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(4)

- (e) What is the equation of directrix of the parabola $y^2 = 16x$?
- (f) Express $\frac{x}{2} + \frac{y}{3} = 1$ in perpendicular form.
- (g) Write down the equation of tangent to the circle $x^2 + y^2 = a^2$ at (x_1, y_1) .
- (h) What are the lengths of major axis and minor axis of the ellipse $9x^2 + 16y^2 = 144$.
- 12. Find the equation of circle passing through the set of points (0, 0), (a, 0) and (0, b). 3
- 13. Find the co-ordinates of the centre, vertices, focii and the equation of the directrices of the hyperbola $9x^2 - 16y^2 = 144$.

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3000(Y)

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