Total No. of printed pages = 10

Sc-102/Maths-I/1st Sem(New)/Com/2017/N

MATHEMATICS - I

(New Course)

Full Marks - 70

Time - Three hours

The figures in the margin indicate full marks for the questions.

PART - A

Choose the correct answer:

1×10=10

- (a) Square root of 3 + 4i is

 - (i) $\pm (4 + i)$ (ii) $\pm (1 + i)$
 - (iii) $\pm (2 i)$ (iv) $\pm (2 + i)$
- (b) Modulus of $\frac{2-i}{3-4i}$ is
 - (i) $\frac{1}{5}$
- (ii) $\frac{1}{\sqrt{5}}$
- .(iii) .√3
- (iv) 5

Tumover

| 1(| (c) | ASI | ne or log | log,log, 81 | 13 | Miren, Botto | |
|-------|---------------|--|------------------------|-------------|------------|--------------|--|
| | rate with the | (i) | 2 | , (ii) | 3 | | |
| | | , (iii) |) 1 | (iv) | None | of the above | |
| | (d) | Val | ue of ω ¹⁰⁵ | is | | | |
| 6 | | (i) | -1 | ·(ii) | 1 | | |
| | Har the Bar | (iii) | ω | (iv) | - ω | | |
| 11 | (e) | arg | (4 - i4) i | s | | | |
| | | (i) | π | (ii) | π/2 | | |
| | | (iii) | π/4 | (iv) | $-\pi/4$ | | |
| | (f) | Sun | of first 2 | 4 terms in | -9 -1 | + 7 + i | |
| | | (i) | 1992 | (ii) | 1662 | | |
| | | (iii) | 4620 | (iv) | None | of the above | |
| | (g) | 6th | term of 2, | 8, 32, | is | | |
| | | (i) | 563 | (ii) | 2408 | | |
| | | (iii) | 4902 | (iv) | 2048 | | |
| 12 | (h) | Number of ways that the letters of the word DEER be arranged is | | | | | |
| | | (i) | 10 | (ii) | 8 | | |
| | | (iii) | 12 | (iv) | 13 | | |
| 45/ - | 45/Sc-102 | /Math | ns-I | (2) | | | |

- (i) Expansion of $(1 + x)^{-1}$ is
 - (i) $1 x + x^2 x^3 + x^4 \dots$ to infinity
 - (ii) $1 + x + x^2 + x^3 + x^4 + \dots$ to infinity
 - (iii) $1 x + x^2 x^3 + x^4 \dots + x^n$
 - (iv) $1 + x + x^2 + x^3 + x^4 + \dots + x^n$
- (j) Cofactor of a_{23} in $\begin{bmatrix} 2 & -1 & 0 \\ 1 & -2 & 1 \\ 4 & 3 & -1 \end{bmatrix}$ is
 - (i) $\begin{vmatrix} 2 & -1 \\ 1 & -2 \end{vmatrix}$ (ii) $\begin{vmatrix} 2 & -1 \\ 1 & -2 \end{vmatrix}$
 - (iii) $-\begin{vmatrix} 2 & -1 \\ 4 & 3 \end{vmatrix}$ (iv) $\begin{vmatrix} 2 & 0 \\ 4 & -1 \end{vmatrix}$
- Choose the correct statement : 1×5=5

- (a) \cdot (i) $\sin^2 x + \cos^2 x = 1$
 - (ii) $\sec^2 x + \csc^2 x = 2$
 - (iii) $\cos^2 x \cot^2 x = -1$
- (b) (i) $-1 < \cos x < 1$ (ii) $\cos x < 1$ (iii) $-1 \le \sin x \le 1$
- 45/Sc-102/Maths-I (3) | Turn over

(c) (i)
$$1 + \sin A = \left(\sin \frac{A}{2} - \cos \frac{A}{2}\right)^2$$

(ii)
$$\cos A = 2\sin^2 \frac{A}{2} + 1$$

(iii)
$$1-\cos A = 2\sin^2\frac{A}{2}$$

tana + tanb + tanc - tana tanb tanc 1-tuna tunb-tunb tunc-tun étana

(ii)
$$tan (a + b) = \frac{tan a - tan b}{1 + tan a tan b}$$

(iii) ten
$$(45^{\circ} + A)$$
 ten $(45^{\circ} - A) = -1$

(e) (i)
$$\frac{a}{\cos A} = \frac{b}{\cos B} = \frac{c}{\cos C}$$

(ii)
$$\cos \frac{A}{2} = \sqrt{\frac{(a-b)(a-c)}{bc}}$$

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| 3. | Find | Find the correct answer: | | | | | | |
|----|------|------------------------------------|------|-------------|----------|--|--|--|
| | (a) | The cost of dig the rate of Rs. | | of size 4 × | 5 × 4 at | | | |
| | | (i) Rs. 4,000 | (ii) | Rs. 2,000 | | | | |

(b) The length of the longest rod that can be kept in a box of size $3 \times 12 \times 4$ is

(i) 7.9 (ii) 8.2

(iii) Rs. 3,500

(iv) Rs. 3,650

(iii) 12.5

(iv) 13

The volume of a sphere of radius 6 is (c)

(i) 287π

(ii) 346π

(iii) 410π

(iv) 288π

(d) The base radius of a cone is 7. If the height of the pyramid is 24 cm, its lateral surface is

(i) 175π (ii) 174

(iii) 238π (iv) 188π

(e) The height of a cylinder is 6 cm and the ratio to its volume to the lateral surface area is 2:1. The radius is

(i) 4.5

(iii) 3

(iii) 4

(iv) 2.5

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(c) (i)
$$1 + \sin A = \left(\sin \frac{A}{2} - \cos \frac{A}{2}\right)^2$$

(ii) $\cos A = 2\sin^2\frac{A}{2} + 1$

(iii)
$$1-\cos A = 2\sin^2\frac{A}{2}$$

(d) (i) tan (a+b+c) =

tuna + tanb + tanc - tana tanb tanc 1-tan a tan b-tan b tan c-tan c tana

(ii)
$$tan(a+b) = \frac{tan a - tan b}{1 + tan a tan b}$$

(e) (i)
$$\frac{a}{\cos A} = \frac{b}{\cos B} = \frac{c}{\cos C}$$

(ii)
$$\cos \frac{A}{2} = \sqrt{\frac{(a-b)(s-c)}{bc}}$$

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4. Choose the correct statement:

- (a) (i) Distance between (4, 1) and (3, 0) is $\sqrt{2}$.
 - (ii) Gradient of the line joining (4, 1) and(3, 0) is 2.
 - (iii) Origin is a point on the line joining (4, 1) and (3, 0).
- (b) (i) Two lines are parallel if coefficient of y in the two equations are same.
 - (ii) Two lines are mutually perpendicular if product of their gradient is 1.
 - (iii) If constant term of an equation of a straight line is 0, then the line passes through the origin.
- (c) (i) The x intercept of 2x 3y + 1 = 0 is 2.
 - (ii) The y intercept of 3x y + 6 = 0 is 6.
 - (iii) 2x 3y + 1 = 0 and 5x 3y + 5 = 0 are parallel lines.
- (d) (i) The gradient form of the equation 2x + y = 4 is y = -2x + 4.
 - (ii) The gradient form of the equation 5x + 2y = 1 is y = -5x + 1.

- (iii) The intercept form of the equation x + y = 6 is $\frac{x}{6} - \frac{y}{6} = 1$.
- (i) Equation of the line passing through (2, 1) and (4, 6) is 5x - 2y = 8.
 - Equation of the line passing through (ii) (0, 0) and (1, 2) is 2x - y = 7.
 - (iii) Equation of the line passing through (-3, 1) and (3, 3) is x + 2y + 6 = 0.

Part - B

- 2×5=10 Answer any five questions:
 - Evaluate log log log 512. (i)
 - If x = 1 i, find the value of $x^2 2x + 2$.
 - (iii) If "P₃ = 336, find "C₃.
 - (iv) Determine the value of k if 7k + 3, 4k 5, 2k + 10 are in AP.
 - (v) Find 8th term in $\left(1+\frac{1}{N}\right)^{12}$.
 - (vi) Apply De Mov's theorem to find the value $(1 + i)^2$.

- (vii) In how many ways can the letters of the word MULTIPLE be arranged without changing the order of the vowels in the word?
- (viii) How many chords can be drawn through 11 points on a circle ?
- 6. Find the value of $(\sqrt{2}+1)^5 (\sqrt{2}-1)^5$. 3
- 7. Answer any two questions: 4×2=8
 - (i) If m is an imaginary cube root of unity, prove that $\frac{1}{1+2m} + \frac{1}{2+m} - \frac{1}{1+m} = 0$.
 - (ii) Insert 5 GMs between 576 and 9.
 - (iii) Prove that $\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^2 & b^2 & c^2 \end{vmatrix} = (a-b)(b-c)(c-a)$
 - (iv) Resolve into simple fraction: $\frac{x^2}{(x+1)^3(x+2)}$
- 8. Prove that (any four): 2×4=8
 - (i) $\sin^2 48^\circ + \sin^2 42^\circ = 1$
- 45/Sc-102/Maths-I (8) 4500(W)

(ii)
$$\tan 53^\circ = \frac{\cos 8^\circ + \sin 8^\circ}{\cos 8^\circ - \sin 8^\circ}$$

I/N

(iii)
$$\tan\left(\frac{\pi}{4} + \frac{\theta}{2}\right) = \sec\theta + \tan\theta$$

(iv)
$$\cos^4\theta - \sin^4\theta = \cos 2\theta$$

(v)
$$\cos 130^{\circ} + \cos 110^{\circ} + \cos 10^{\circ} = 0$$

(vi)
$$\frac{\cos\theta + \cos\phi}{\sin\theta - \sin\phi} = \frac{\sin\theta + \sin\phi}{\cos\phi - \cos\theta}$$

(vii)
$$\frac{\sin(B-C)}{\cos B \cos C} = \tan B - \tan C$$

9. Answer any two questions:

- If A + B + C = π , prove that $\sin^2 A + \sin^2 B$ $+ \sin^2 C = 2 + 2\cos A \cos B \cos C$
- (ii) Prove that $\tan^{-1} \frac{5}{12} = \sin^{-1} \frac{5}{13} = \cos^{-1} \frac{12}{13}$
- (iii) For the triangle ABC, prove that $\tan \frac{A-B}{2} = \frac{a-b}{a+b} \cot \frac{C}{2}$

45/Sc-102/Maths-I (9) Turn over

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10. A river is 32m wide. The depth d in meters at a distance x m from one bank is given by the following table:

| - | x : | 0 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 |
|---|-----|---|----|----|----|----|----|----|----|----|
| | d : | 0 | 10 | 20 | 25 | 30 | 41 | 44 | 26 | 10 |

Find the approximate cross-section of the river. 3

11. Answer any two questions:

 $2 \times 2 = 4$

- (i) Show that (-1, -1), (1, 1) and $(-\sqrt{3}, \sqrt{3})$ are the vertices of an equilateral triangle.
- (ii) Divide the line joining (-1, 1) and (6, 8) internally in the ratio 2:1.
- (iii) Find locus of a point moving at a constant distance 3 from (4, 1).
- (iv) Find the length of perpendicular from (0, 0) to x 5y 9 = 0.
- 12. Find the angle between the lines x + 2y 1 = 0 and 6x + 5y 3 = 0.

Or

Show that the points (2, 3) (3, 5) and (6, 11) and collinear.