Total No. of printed pages = 5 Sc-102/Maths-I/1st Sem/Comm/2017/M

(2) Write down the oil term of (3x + 1/x)?

MATHEMATICS - I

Full Marks – 70 Pass Marks – 21

Time - Three hours

The figures in the margin indicate full marks for the questions.

GROUP – A. (Algebra)

1. Answer any seven questions : 7×2=14

(a) Prove that $\sqrt{i} + \sqrt{-i} = \sqrt{2}$

(b) If $x + y \alpha x - y$, prove that $x \alpha y$.

(c) Insert 3 Arithmetic Mean between 3 and 23.

- (d) Find the base of the logarithm of 1728 is 6.
- (e) Find the value of $x^3 2x^2 7x + 8$, when $x = 2 + \sqrt{3}$.

[Turn over

- (f) Find the modulus of $\frac{12+5i}{24+7i}$
 - (g) Write down the 6th term of $(3x + \frac{1}{2}y)^9$
 - (h) If x varies directly as y and inversely as z and x = a, when y = b, z = c. Find the value of x, when $y = b^2$, $z = c^2$.
 - 2. Prove that :
 - leures in the margin indicate full man
 - (a) $x^{\log y \log z} \times y^{\log z \log x} \times z^{\log x \log y} = 1$
 - (b) If α and β be the roots of $2x^2 + 3x + 7 = 0$, find the values of $\alpha^2 + \beta^2$. $3\frac{1}{2} \times 2 = 7$
 - 3. (a) If 'r' be the ratio of the roots of $ax^2 + bx$

+ c = 0, then prove that $\frac{(r+1)^2}{r} = \frac{b^2}{ac}$.

(b) Find the coefficient of x^{11} in $\left(x + \frac{2}{x^2}\right)^{17}$ $3\frac{1}{2} \times 2 = 7$

(2)

48/Sc-102/Maths-I

4. (a) Show that

$$\begin{vmatrix} 1 & 1 & 1 \\ a & b & c \\ a^2 & b^2 & c^2 \end{vmatrix} = (a - b) (b - c) (c - a)$$

(b) Using Cramer's rule, solve : $3\frac{1}{2}\times2=7$ x + y + z = 3 . The prove that (a) . 2x - y + 3z = 4x + 2y - z = 2

GROUP – B

sin 2A + sin 2P + vin 2C = 4 snA , sinib. sinC Answer any four questions. $4 \times 5 = 20$

5. (a) Evaluate 2¹/₂

(i) cosec (-765°)

(ii) tan (780°).

(a) Prove that ten - wind avoid (a) (b) Prove that :

21/2

 $\frac{\sin (B-C)}{\cos B. \cos C} + \frac{\sin (C-A)}{\cos C. \cos A} + \frac{\sin (A-B)}{\cos A. \cos B} = 0$

48/Sc-102/Maths-I (3) [Turn over

6. (a) Prove that

 $\cos 130^\circ + \cos 110^\circ + \cos 10^\circ = 0$

(b) $\cos 20^\circ \cos 40^\circ \cos 60^\circ \cos 80^\circ = \frac{1}{16}$.

7. (a) Prove that $\sin 3\theta = 3 \sin \theta - 4 \sin^3 \theta$

(a - b) (a - c) (d - a) = a

- (b) Find the value of sin 18°.
- 8. (a) If $A + B + C = \pi$, prove that $\sin 2A + \sin 2B + \sin 2C = 4 \sin A \cdot \sin B \cdot \sin C$ 2
- (b) The angle of elevation of the top of a tower at a distance of 400 metres from its foot is 60°. Find the height of the tower. 3

9. (a) Prove that
$$\tan^{-1} \frac{1}{2} + \tan^{-1} \frac{1}{3} = \pi/4$$

(b) In any triangle, prove that

$$\tan \frac{B-C}{2} = \frac{b-c}{b+c} \cdot \cot \frac{A}{2}$$

48/Sc-102/Maths-I

(4)

2000(G)

3

2

3

2

3

GROUP - C

10. Answer any three from the following : $3 \times 5 = 15$

(a) Find the volume and curved surface of a right circular cone whose height is 8 cm and the radius of the circular base is 3 cm.

- (b) A cylindrical oil tanker has its inner diameter 480 cm. If the length of the tanker is 6m, find the capacity of the tanker is c.c.
- (c) Find by Simpson's rule the area of a curvilineal figure whose ordinates measure 18, 22, 26, 24, 20, 26, 30, 34, 28, 24 and 14 cm and whose base is 146 cm.
- (d) Find the volume of the frustum of a pyramid the areas of whose ends are 32 sq.m and 20 sq.m and height is 6m.

2000(G)