

2023

**Optimization Techniques in Water Resources Engg**

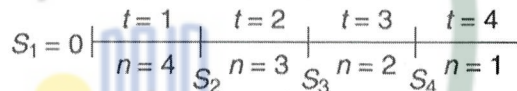
Full Marks: 100

Time: 3 hours

*The figures in the margin indicate full marks for the questions.*

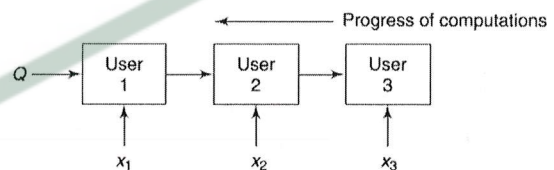
1. Inflows during four seasons to a reservoir with storage capacity of 4 units are, respectively, 2, 1, 3 and 2 units. Overflows from the reservoir are also included in the release. Reservoir storage at the beginning of the year is 0 units. Release from the reservoir during a season result in the following benefits which are same for all the four seasons. Obtain the release policy of the reservoir using dynamic programming. 20

Release	Benefits
0	-100
1	250
2	320
3	480
4	520
5	520
6	410
7	120



2. A total of 6 units of water is to be allocated optimally to three users. The allocation is made in discrete steps of one unit ranging from 0 to 6. With the three users denoted as User 1, User 2 and User 3 respectively, the returns obtained from the users for a given allocation are given in the following table. find allocations to the three users such that the total return is maximized. 20

Amount of Water Allocated $x$	Return from		
	User 1 $R_1(x)$	User 2 $R_2(x)$	User 3 $R_3(x)$
0	0	0	0
1	5	5	7
2	8	6	12
3	9	3	15
4	8	-4	16
5	5	-15	15
6	0	-30	12



3. Minimize  $f(x) = 5x_1^2 + x_2^2 + 4$  20  
 Subject To,  $x_2 - 4 \geq -4x_1$  ;  $-x_2 + 3 \leq 2x_1$

4. Minimize  $f(x) = 5x_1^2 + 2x_2 - x_1x_2$  20  
 Subject To,  $x_1 + x_2 = 3$

5. Maximize  $Z = 2x_1 + x_2$  20  
 Subject To,  $3x_1 + x_2 \leq 300$  ;  $4x_1 + 2x_2 \leq 500$ ,  $x_1, x_2 \geq 0$