2012 C 2013 (May)

NUMERICAL METHODS AND COMPUTER PROGRAMMING

Paper: MA 401

Full Marks: 100

Pass Marks: 30

Time: Three hours

The figures in the margin indicate full marks for the questions.

Answer any five questions.

- 1. (a) What do you mean by relative error? Find the absolute error and the relative error if the number X = 0.004997 is rounded off to three decimal digits.
 - (b) The area A of a circle of diameter 'd' is given by the following values: 5

 d: 80 85 90 95 100

 A: 5026 5674 6362 7088 7854

 Find the approximate value for the area of circle of diameter 82.

(c) A slider in machine moves along a fixed straight rod. Its distance x cm along the rod is given below for various values of the time t seconds. Find the velocity of the slider and its acceleration when t = 0.3 seconds 10

t: 0 0.1 0.2 0.3 0.4 0.5 0.6

x: 30.13 31.62 32.87 33.64 33.95 33.81 33.24

- 2. (a) Write the algorithm of Lagrange's interpolation formula.
 - (b) Compute the value of $\int_{0.2}^{1.4} (\sin x \log x + e^x) dx$ using Simpson's $\frac{3}{8}$ th rule by taking seven ordinates.
- The pressure and the volume of a gas are related by the equation $PV^{\gamma} = K$; γ and K being constants. Fit the equation to the following set of observations:

 $P(kg/cm^2)$: 0.5 1.0 1.5 2.0 2.5 3.0 V(litres): 1.62 1.00 0.75 0.62 0.52 0.46

3. (a) Write the geometrical interpretation of Newton-Raphson's method.

(b) Using Lagrange's formula find the form of the function given by

x : 3 2 1 -1

f(x): 3 12 15 -21

- formula and the value of 748) in Solve the following equations by Gauss-Seidal iteration method to correct four decimal places, $7x_1 + 52x_2 + 13x_3 = 104$; $83x_1 + 11x_2 - 4x_3 = 95$; $3x_1 + 8x_2 + 29x_3 = 71$ 10
- 4. (a) Using Regula-Falsi method, find the real root of $e^x = 4 \sin x$ correct to three decimal places.

Given, x: 1 2 3 4 5 6 7 8 f(x): 1 8 27 64 125 216 343 512

Find f(7.5). 5

(c) Using Runge-Kutta method of fourth order, solve $\frac{dy}{dx} = xy + y^2$ with y(0) = 1 at x = 0.1, 0.2, 0.310

- 5. (a) Using Bisection method, find the root of the equation $\cos x = xe^x$ correct to three decimal places.
 - By means of Newton's divided difference formula find the value of f(8) from the following table:

x: 4 5 7 10 11 13 f(x): 48 100 294 900 1210 2028

- (c) Using Milne's method, find y(2) if y(x) is the solution of $\frac{dy}{dx} = \frac{1}{2}(x+y)$ given that y(0) = 2, y(0.5) = 2.636, y(1) = 3.595, y(1.5) = 4.968
- 6. (a) Using Gauss elimination method, solve the equations:

$$3x_1 + 2x_2 - 2x_3 = -2$$

$$2x_1 + 4x_2 + x_3 = 3$$

$$x_1 - x_2 + x_3 = 6$$

(b) Using three point Gaussian quadrature formula evaluate $\int_0^1 \frac{dx}{1+x}$.

- (c) Solve the differential equation $\frac{dy}{dx} xy = 0$; y(0) = 1 from x = 0 to x = 0.25 using Euler's method.
- 7. (a) Fit a second degree Parabola to the following data:

$$x = 1.0$$
 1.5 2.0 2.5 3.0 3.5 4.0 $y = 1.1$ 1.3 1.6 2.0 2.7 3.4 4.1

Write an algorithm to implement Euler's Improve method. Using Euler's Improve method, find y at x = 0.1 and x = 0.2 given

that
$$\frac{dy}{dx} = y - \frac{2x}{y}$$
, $y(0) = 1$. $4+8=12$