2017

THEORY OF COMPUTATION

Paper: IT 503

Full Marks: 100

Time: Three hours

The figures in the margin indicate full marks for the questions.

Answer any five questions.

- 1. (a) Prove that $L = \{0^n 1^n | n \ge 1\}$ is not regular.
 - (b) Define \in closure of a state with example. Prove that $Q + RP = QP^*$.

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- 2. (a) Write regular expressions for the following:
 - (i) Binary members that are multiple of 2.

- (ii) Strings of a's and b's with no consecutive a's
- (iii) Strings of a's and b's containing consecutive a's.
 - (b) Construct a finite state machine that accepts exactly those input strings of 0's and 1's that ends with 11.
 - (c) Design FA which accepts even number of 0's and even member of 1's. 5
- 3. (a) Find L(G) for CFG $S \to aSb \mid aAb, A \to bAa, A \to ba$ 5
 - (b) Convert an NFA to a DFA given NFA $M = \left(\Sigma, Q, S, q_0, F\right), \quad \Sigma = \{0, 1\},$ $Q = \left\{q_0, q_1, q_2, q_3\right\}, \quad F = \left\{q_0\right\}$

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(c) Convert the following grammar G in GNF form $S \rightarrow ABb|a$, $A \rightarrow aaA|B$, $B \rightarrow bAb$

4. (a) Show that id+id*id can be generated by two distinct leftmost derivation in the grammar

$$E \rightarrow E + E \mid E * E \mid (E) \mid id$$
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(b) Let
$$G = (N, T, P, S)$$
,
$$P = \{S \to A1B \mid a, A \to OA \mid \epsilon, B \to OB \mid 1B \mid \epsilon\}$$
Give a leftmost and rightmost derivation for the string $00 \mid 0 \mid$.

(c) Construct a minimum state automaton equivalent to the following transition system.

State	Input		
	a a	b	
$\rightarrow q_0$	q_0	q_3	
q_1	q_2	95	
q_2	q_3	q_4	
q_3	q_0	q_5	
q_4	q_0	q_{6}	
q_5	q_1	q_4	
96	q_1	q_3	

5. (a) Define Pushdown Automaton. What are the different ways of language acceptances by a PDA and define them.

2+3=5

(b)	Convert the given expression to PDA	
- /	$I \rightarrow a b Ia Ib I0 I1$	5
(c)	Which is more powerful <i>NFA</i> or <i>PDA</i> Justify your answer with example.	?
111	P IS - ALB a A - OA S B - OB	J
(d)	State the pumping lemma for CFL's.	
1	for the string 00 0 .	5
Wri	te short notes on : 4×5=2	0
(a)	Chomsky Hierarchy	
(b)	Context Sensitive Language	
(c)	Turing Machine	
(4)	Mealy and Moore Machine	

6.

entire by a PDA and define them