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53 (IE 604) CNSY-II

2021

CONTROL SYSTEM-II

Paper : IE 604

Full Marks : 100

Time : Three hours

The figures in the margin indicate full marks for the questions.

Answer **any five** questions.

1. (a) Draw and explain the Bode plot for a phase lead network. 8

(b) Design a suitable lead compensating

network for $G(s) = \frac{K}{s(s+1)(s+20)}$ to

fulfill the following specifications :

Velocity error constant (K_v) = 20 sec^{-1} ;

Phase margin (PM) $\geq 35^\circ$,

Assume the margin of safety = 5° .

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Contd.

2. (a) Explain the phase plane technique. 10
- (b) How can time be determined from the phase plane trajectory? 10
3. (a) Define : 7
- (i) Non-linear system;
- (ii) The describing function.
- (b) What are the common types of nonlinearities? 3
- (c) Determine the describing function for a practical relay. 10
4. (a) Define state variable, state vector and state space. 6
- (b) What are the advantages of state space technique? 4
- (c) A system is described by the differential equation —

$$\frac{d^3y}{dt^3} + 5\frac{d^2y}{dt^2} + 7\frac{dy}{dt} + 9y = 11u_1(t) + 13u_2(t)$$

where, $y(t)$ is the output and $u_1(t)$,

$u_2(t)$ are the inputs to the system. Obtain the state space representation of the system. 10

5. (a) State and prove the Final value theorem (FVT) for Z-transformation. 8

(b) Find the final value of $f(k)$ using FVT for a given function : 6

$$F(z) = \left(\frac{1}{1-z^{-1}} \right) - \left(\frac{1}{1-e^{-aT}z^{-1}} \right)$$

(c) Solve the following difference equation using Z-transform method : 6

$$x(k+2) + 3x(k+1) + 2x(k) = 0$$

Assume, $x(0) = 0$ and $x(1) = 1$.

6. (a) A control system is described by the following matrices : 10

$$A = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ 0 & -2 & -3 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad \text{and} \quad C = [1 \ 2 \ 0]$$

Determine the transfer function of the system.

- (b) A single input-single output (SISO) system is represented as: 10

$$x(t) = \begin{bmatrix} -2 & 0 & 0 \\ 0 & -3 & 0 \\ 0 & 0 & -4 \end{bmatrix} x(t) + \begin{bmatrix} 1 \\ 1 \\ 0 \end{bmatrix} u(t)$$

$$\text{and } y(t) = [1 \ 0 \ 2] x(t).$$

Test the controllability and observability of this SISO system.

7. (a) What is transfer matrix and state transition matrix? 10

- (b) Compute the state transition matrix when

$$A = \begin{bmatrix} -1 & 1 \\ 0 & 2 \end{bmatrix} \quad 10$$

8. Write short notes on: **(any two)** $10 \times 2 = 20$

- (i) Design procedures for phase lag compensation
- (ii) Properties of state transition matrix
- (iii) Stability analysis from the phase plane trajectory.

