

2017

**CONTROL SYSTEM-I**

Paper : IE 503

Full Marks : 100

Time : Three hours

**The figures in the margin indicate full marks for the questions.**

Answer **any five** questions out of **seven**.

1. (a) Reduce the block diagram shown in Fig. (1a) and obtain the overall transfer function. 10

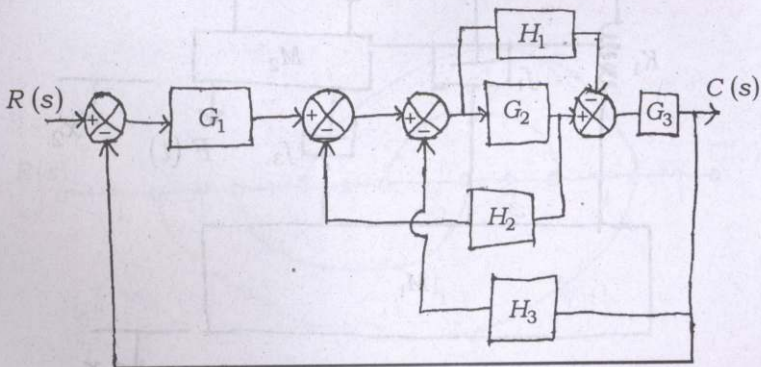


Fig. (1a)

Contd.

- (b) A unity feedback system is characterised by an open loop transfer function

$$G(s) = \frac{K}{s(s+1)(s+2)}$$

Determine the error at steady state for input,  $r(t) = 5t$  and  $K = 10$ .

Also find  $K$  for  $e_{ss} = 0.2$ .

5

7.

- (c) Write the differential equations for the mechanical system shown in Fig. (1c). Also obtain the analogous electrical circuit based on force-current analogy.

5

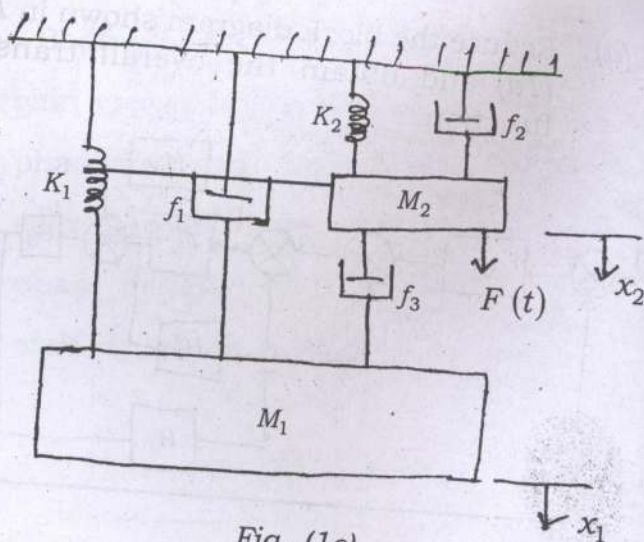


Fig. (1c)

2. (a) Define the following : 2+2

(i) Non-touching loop of a signal flow graph.

(ii) Take off point of a block diagram.

(b) The characteristic equation of a feedback control system is given by

$$s^4 + 20ks^3 + 5s^2 + 10s + 15 = 0$$

By applying Routh criterion determine the range of values of  $K$  for the system to be stable. 5

(c) Consider the signal flow graph of Fig. (2c). Obtain the overall transfer function

function  $\frac{C(s)}{R(s)}$  using Mason's gain formula.

formula. 6

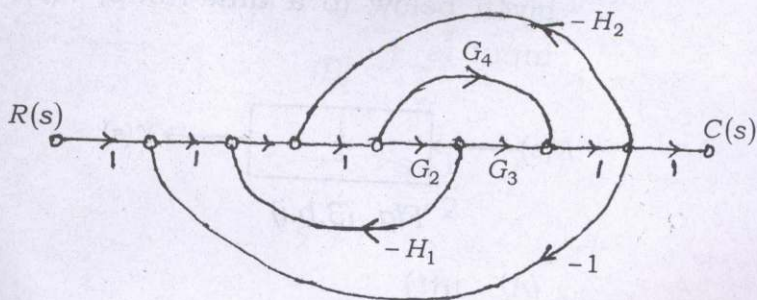


Fig. (2c)

(d) Define the following : 5

- (i) Peak overshoot
- (ii) Rise time w.r.t. a second order unit steps input system.

3. (a) Write short notes on: **(any two)** 2×5

- (i) Synchro
- (ii) P-D control action
- (iii) Servomotor.

(b) Choose the correct alternatives from the following : 2×5

- (i) Assuming zero initial condition, the response  $y(t)$  of the system given below to a unit ramp,  $r(t)$  input is

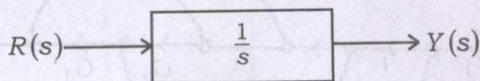


Fig. (3.b.i)

- (A)  $u(t)$
- (B)  $tu(t)$

(C)  $\frac{t^2}{2}u(t)$

(D)  $e^{-t}u(t)$

(ii) The transfer function  $V_2(s)/V_1(s)$  of the circuit shown below is

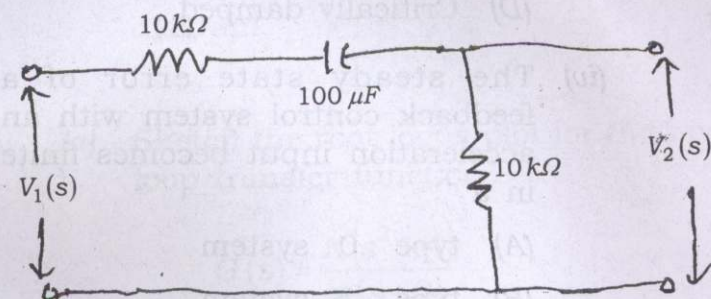


Fig. (3.b.ii)

(A)  $\frac{s+1}{s+2}$

(B)  $\frac{s+1}{10^4}$

(C)  $\frac{s+1}{s+2}$

(D)  $\frac{10^4}{s+1}$

- (iii) If the characteristics equation of a system is,  $s^2 + 4s + 10 = 0$ , the system is
- (A) undamped
  - (B) Over damped
  - (C) Under damped
  - (D) Critically damped.
- (iv) The steady state error of a feedback control system with an acceleration input becomes finite in a
- (A) type 0 system
  - (B) type 1 system
  - (C) type 2 system
  - (D) type 3 system
- (v) For the transfer function  $\frac{K}{(s+1)(s+2)(s+3)}$  the root locus break away point will be \_\_\_\_\_.
- (A) between 0 and -1
  - (B) between -1 and -2
  - (C) between -2 and -3
  - (D) beyond -3.

4. (a) Sketch the polar plot of the system :

$$G(s) = \frac{10}{s(1+s)(.5+2s)} \quad 10$$

- (b) Discuss the effect of the PMDC motor with armature control. Draw the necessary transfer function and block diagram. 10

5. (a) Sketch the root locus plot for the open loop transfer function —

$$G(s) = \frac{K(s^2 + 4)}{s(s+2)}$$

Calculate the value of  $K$  at,

(i) break away point

(ii)  $s = -0.69 + j0.9$

(iii) marginal stability.

14+2+2+2

6. (a) Plot the Nyquist plot to determine the phase margin and gain margin for

$$G(s)H(s) = \frac{K}{s(0.4s+1)(0.2s+1)}$$

10+4

- (b) The overall transfer function of a system is given by

$$\frac{C(s)}{R(s)} = \frac{25}{s^2 + 7s + 25}$$

Find all the time response specification and the expression for output. 6

7. Sketch the asymptotic Bode plot for the transfer function given below —

$$G(s)H(s) = \frac{10}{s(s+1)(s+2)}$$

From the Bode plot determine

- (i) the gain crossover frequency
- (ii) the phase crossover frequency
- (iii) the gain margin
- (iv) the phase margin
- (v) the stability of the system.

10+10