53 (CS 503) DAAL

2016

DESIGN AND ANALYSIS OF ALGORITHM

Paper: CS 503

Full Marks: 100

Time: Three hours

The figures in the margin indicate full marks for the questions.

Answer any five questions.

- 1. (a) Prove that quick sort suffers in worst case complexity when an array is sorted and the key element is the first or last element of the array.
 - (b) Compute the time complexity for the following recursive relation

$$T(n) = T(n/2) + c$$
 15+5

2. A number of processes want to execute by minimum number of processors. Design a greedy algorithm for this situation.

Apply your algorithm on the following processes.

	P_1	P_2	P_3	P_4	P_5	P_6	P_7	P_8	P_9	P_{10}
Arrival Time	1	2	3	5	5	4	6	8	9	11
Finish Time	3	4	6	7	9	8	9	10	11	13

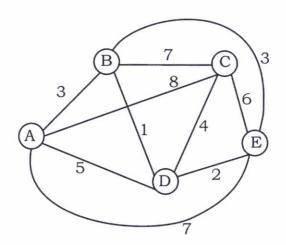
3. Write down the CUT_ROD problem. Consider the following example:

Size	1	2	3	4
Profit	5	8	9	6

Draw the recursive tree (sequence of calls should be mentioned clearly) for brute force approach and dynamic programming. Compute the complexity for both the cases.

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4. Consider the following TSP problem. Use branch and bound to compute the optimized cost.



- 5. With an example prove that greedy algorithm cannot produce optimal solution (always) for 0/1 knapsack whereas for fractional knapsack it always produce optimal solution.
- 6. (a) Discuss about Cooks theorem.
 - (b) If Hamiltonian cycle is NP complete then TSP problem is NP complete.
 - (c) Prove that 2 SAT is not NP complete. 5+5+10