

Total number of printed pages—4

53 (CS 502) THCM

2017

THEORY OF COMPUTATION

Paper : CS 502

Full Marks : 100

Time : Three hours

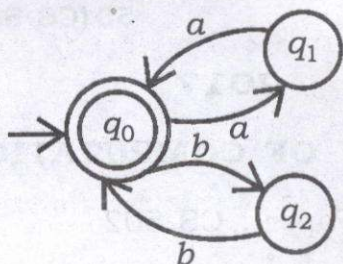
The figures in the margin indicate full marks for the questions.

Answer **any five** questions.

1. 2×10
- (a) What do you mean by non-regular language ?
- (b) Regular language is represented by —
- (i) DFA
 - (ii) NFA
 - (iii) Regular expression
 - (iv) Regular grammar.
- (c) Write a DFA or NFA for the regular expression $r = \epsilon + a^+$.

Contd.

(d) Write the regular expression of



(e) Arrange according to the computational power :

NFA, DFA, NPDA, DPDA, TM.

(f) Is the language is regular ?

$$L = \{a^m b^n : m, n \geq 0 \text{ and } m \neq n\}$$

(g) State the pigeonhole principle.

$$(h) L = \{awbwa : w \in \{a, b\}^*\}$$

Write all the strings in L of length ≤ 5 .

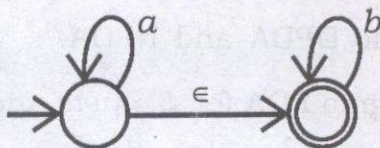
(i) Explain the input and output of a DFA.

(j) Define indistinguishable state in DFA.

2. (a) Write a DFA or NFA of

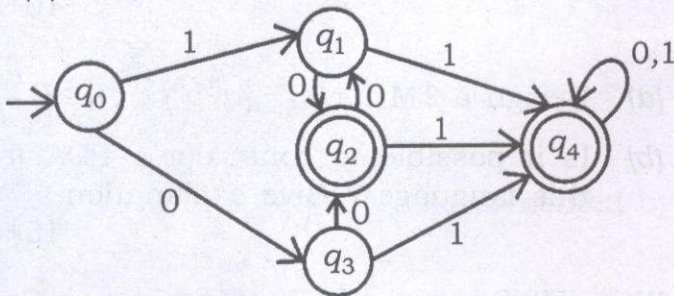
$$L = \{aw_1w_2a : w_1, w_2 \in \{a, b\}^*\}.$$

- (b) Write a regular expression of
 $L = \{awa \text{ or } bwb : w \in \{a,b\}^*\}$.
- (c) Write a grammar of
 $L = \{a^n b^m c^n : m, n \geq 0\}$.
- (d) Convert the ϵ -NFA to equivalent ϵ -free NFA.



5+5+5+5

3. (a) Minimize the DFA



- (b) State and prove the pumping lemma of regular language.
- (c) Prove that $L = \{a^n b^n : n \geq 0\}$ is not regular.

5+10+5

4. (a) Define CNF and GNF.
 (b) Convert the grammar into CNF
 $S \rightarrow bA|aB$, $A \rightarrow bAA|aS|a$,
 $B \rightarrow aBB|bS|b$.
 (c) Define ambiguous and un-ambiguous grammar with example.

5+10+5

5. (a) Define DPDA and NPDA.
 (b) Design a PDA for $L = \{ww^R : w \in \{a,b\}^*\}$.
 (c) Give an example of language which is recognized by NPDA but not DPDA with explanation.

5+10+5

6. (a) Design a TM for $L = \{a^n b^n c^m : n \geq 0\}$.
 (b) Is it possible to construct a PDA for this language? Give explanation.

15+5

7. Write short notes on :

5×4

- (a) Universal TM
 (b) Recursive and Recursively enumerable language
 (c) Primitive Recursive Function
 (d) Church-Turing Thesis.