53 (IE 403) LSAS

2017

LINEAR SYSTEM AND SIGNALS

Paper: IE 403

Full Marks: 100

Time: Three hours

The figures in the margin indicate full marks for the questions.

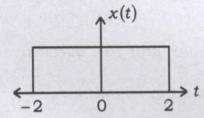
Answer any five questions.

- 1. (a) Define the following:
 - (i) Deterministic signal
 - (ii) Causal system
 - (iii) Memoryless system
 - (iv) Unit step signal
 - (v) Unit impulse signal and
 - (vi) Linear system.

6

(b) Determine whether the following signals are periodic or not, if periodic find out the fundamental frequency —

- (i) $2ws5\pi t + sin3\pi t$
- (ii) e^{j3n}
- (c) Draw the following signals 2×2=4
 - (i) 3u(t-3)
 - (ii) $x\left(\frac{t}{2}+3\right)$ if



(d) Evaluate the following — 2×3=6

(i)
$$\sum_{n=-2}^{5} e^{3n} \delta(n-4)$$

- (ii) $\int_0^t t^2 \delta(t-3) dt$
- (iii) $\int_0^3 \delta(t) \sin 5\pi t \, dt$

2. (a) Test the linearity, time invariance and causality of the following signal

$$y(t) = 2x(t) + 4$$

(b) Find the convolution of — 2×4=8

(i)
$$e^{-2t}u(t)*e^{-4t}u(t)$$

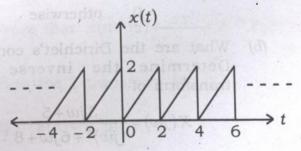
(ii)
$$\cos u(t) * u(t-3)$$

(c) Determine the convolution of following using graphical and matrix method — 4+2=6

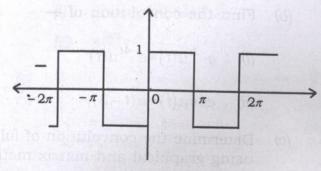
$$x_1[n] = [2, 5, 6, 7]$$

$$x_2[n] = [1, 4, 3]$$

3. (a) Find the trigonometric Fourier series for the following signal:



- (b) Prove the linearity and time shifting property of Fourier series.
 - (c) Obtain the exponential Fourier series for the following waveform 7



- 4. (a) Derive the Fourier transform of the following signals 3×4=12
 - (i) $\sin w_0 t u(t)$
 - (ii) $e^{-t} \sin 5t u(t)$
 - (iii) $x(t) = 1 t^2$; 0 < t < 1= 0, otherwise
 - (b) What are the Dirichlet's conditions?

 Determine the inverse Fourier transform of 2+6=8

$$X(jw) = \frac{3jw + 5}{(jw)^2 + 6jw + 8}$$

- 5. (a) What are the conditions for the existence of Laplace transform? Write the advantages of Laplace transform.

 2+2=4
 - (b) Determine the L.T. and the ROC of the following signals 2×4=8

(i)
$$x(t) = e^{-t}u(t) + e^{-5t}u(t)$$

(ii)
$$x(t) = t^2 u(t)$$

(c) Find the inverse Fourier transform of the following — 2×4=8

(i)
$$X(s) = \frac{s+4}{s^2+5s+6}$$

(ii)
$$X(s) = \frac{s^2 + 1}{s(s+1)(s+2)}$$

- 6. (a) Prove that $x(n-m) \stackrel{Z.T.}{\longleftrightarrow} Z^{-m}X(Z)$
 - (b) Find the Z-transform of

(i)
$$x(n) = a^n u(n)$$

(ii)
$$x(n) = b^n u(-n-1) + (0.5)^n u(n)$$

3+5=8

(c) Determine the inverse Z-transform of

$$X(z) = \frac{z}{2z^2 - 3z + 1}$$
; ROC $|z| > 1$

8

- 7. (a) Define the sampling theorem? What is the nyquist frequency and nyquist interval? What is the basic function of sampling? 2+1+1=4
 - (b) What are the effects of undersampling?
 With necessary diagram explain the operation of impulse and natural sampling.

 2+4+4=10
 - (c) Determine the nyquist frequency and interval for the following 3+3=6

(i)
$$x(t) = \sin c^2 100 \pi t$$

(ii)
$$x(t) = 10 \sin 40 \pi t \cos 60 \pi t$$