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53 (IE 503) CNSY-I

2014

CONTROL SYSTEM-I

Paper : IE 503

Full Marks : 100

Pass Marks : 30

Time : Three hours

The figures in the margin indicate full marks for the questions.

Answer any five questions out of seven.

1. (a) For the system represented by the following equations, find the transfer function $\frac{X(S)}{F(S)}$ by signal flowgraph technique 5

$$x = x_1 + \beta_3 u$$

$$\dot{x}_1 = -\alpha_1 x_1 + x_2 + \beta_2 u$$

$$\dot{x}_2 = -\alpha_2 x_1 + \beta_1 u$$

Contd.

- (b) Reduce the block shown in Fig. (1.b) and obtain the overall transfer function 10

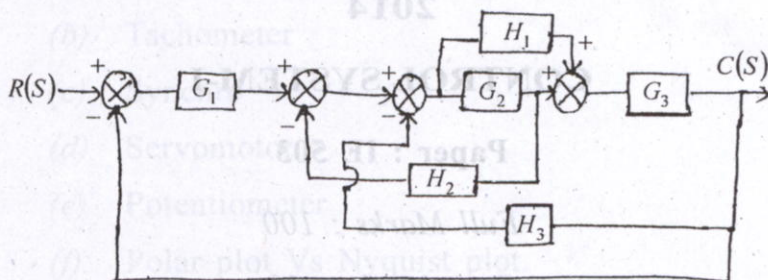


Fig. (1.b)

- (c) Obtain the transfer function of the mechanical system shown in Fig.(1.c). 5

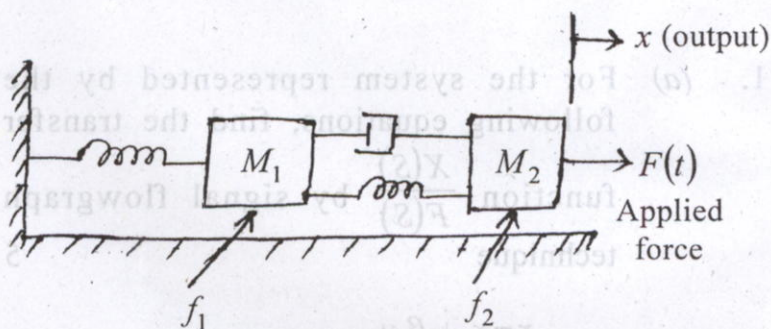


Fig. (1.c)

2. (a) A positional servomechanism is characterised by an open loop transfer function

$$G(S) = \frac{K}{S(S + \alpha)}, \text{ where } K \text{ and } \alpha \text{ are}$$

positive constants, for an unity feedback. Find the values of K and α for a damping co-efficient value of 0.6 and damped frequency of 8 rad/sec. Also find the peak value of the response when the system is excited by a step of 2 volts. 10

- (b) Using Routh's criterion, check the stability of the system equation of 5

$$S^6 + 2S^5 + 8S^4 + 12S^3 + 20S^2 + 16S + 16 = 0$$

- (c) Obtain expressions for peak time and maximum overshoot for a second-order feedback system response for a step input. 5

3. (a) Sketch the polar plot of the system given by

$$G(S) = \frac{10}{S(S+1)(S+5)} \quad 10$$

- (b) The open loop transfer function of a servo system with unity feedback is

$$G(S) = \frac{10}{S(0.1S + 1)}$$

Evaluate the static error-coefficient (K_a, K_u, K_p) for the system. Obtain the steady state error of the system when subjected to an input given by the polynomial $r(t) = a_0 + a_1 t + \frac{a_2}{2} t^2$ 10

4. (a) Sketch the root locus plot for the open loop transfer function

$$G(S)H(S) = \frac{K(S^2 + 4)}{S(S + 2)}$$

Calculate the value of K at breakaway point. 15

- (b) Why root locus technique is required in control system engineering ?
What are the basic conditions to sketch the root locus ? 5

5. (a) Sketch the asymptotic Bode plot for the transfer function given below —

$$G(S)H(S) = \frac{2(S + 0.25)}{S^2(S + 1)(S + 0.5)}$$

From the Bode plot determine —

- (i) the phase cross-over frequency
- (ii) the gain cross-over frequency
- (iii) the gain margin
- (iv) the phase margin

Is the system stable ?

20

6. (a) State the Nyquist stability criterion and explain with example. 5

- (b) Draw the Nyquist plot for the system whose open loop transfer function is

$$G(S)H(S) = \frac{6S + 1}{S^2(S + 1)(3S + 1)} \quad 15$$

7. Write short notes : (*any four*) 4×5

- (a) Proportional and Integral action
- (b) Tachometer
- (c) Synchro
- (d) Servomotor
- (e) Potentiometer
- (f) Polar plot Vs Nyquist plot.